

A. Nokrane and T. J. Ransford, **Schwarz's Lemma for Algebroid Multifunctions**, *Complex Variables Theory Appl.*, 45 (2001), 183–196.

**Abstract**

Let  $U = \{z \in \mathbf{C} : |z| < 1\}$ , let  $a_1, \dots, a_n$  be holomorphic functions on  $U$ , and set

$$F(z) = \{w \in \mathbf{C} : w^n + a_1(z)w^{n-1} + \dots + a_{n-1}(z)w + a_n(z) = 0\} \quad (z \in U).$$

We show that

$$\Delta_\tau(F(z_1), F(z_2)) \leq \tau(z_1, z_2)^{1/n} \quad (z_1, z_2 \in U),$$

where  $\Delta_\tau$  denotes the Hausdorff distance between two sets, measured with respect to the hyperbolic pseudo-metric  $\tau$  on  $U$ . We further show that

$$D_\tau(F(z_1), F(z_2)) \leq k(\tau(z_1, z_2)^{2/n}) \quad (z_1, z_2 \in U),$$

where  $D_\tau$  denotes the matching distance between two  $n$ -tuples, again measured with respect to  $\tau$ , and where  $k$  is the elliptic modulus function. Two examples are given relating to the sharpness of these inequalities.